

# Abstract

Let  $G$  be a simple algebraic group and let  $G^\vee$  be its Langlands dual group. Barbasch and Vogan based on earlier work of Lusztig and Spaltenstein, define a duality map  $D$  that sends nilpotent orbits  $\mathbb{O}_{e^\vee} \subset \mathfrak{g}^\vee$  to special nilpotent orbits  $\mathbb{O}_e \subset \mathfrak{g}$ . In a work by Losev, Mason-Brown and Matvieievskyi, an upgraded version  $\tilde{D}$  of this duality is considered, called the refined BVLS duality.  $\tilde{D}(\mathbb{O}_{e^\vee})$  is a  $G$ -equivariant cover  $\tilde{\mathbb{O}}_e$  of  $\mathbb{O}_e$ . Let  $S_{e^\vee}$  be the nilpotent Slodowy slice of the orbit  $\mathbb{O}_{e^\vee}$ . The two varieties  $X^\vee = S_{e^\vee}$  and  $X = \text{Spec}(\mathbb{C}[\tilde{\mathbb{O}}_e])$  are expected to be symplectic dual to each other. In this context, a version of the Hikita conjecture predicts an isomorphism between the cohomology ring of the Springer fiber  $\mathcal{B}_{e^\vee}$  and the ring of regular functions on the scheme-theoretic fixed point  $X^T$  for some torus  $T$ . This conjecture holds when  $G$  is of type A. In this talk, I will discuss the statuses of similar statements about the Hikita conjecture for general  $G$ . Part of the result is based on a joint work with Vasily Krylov and Dmytro Matvieievskyi.